

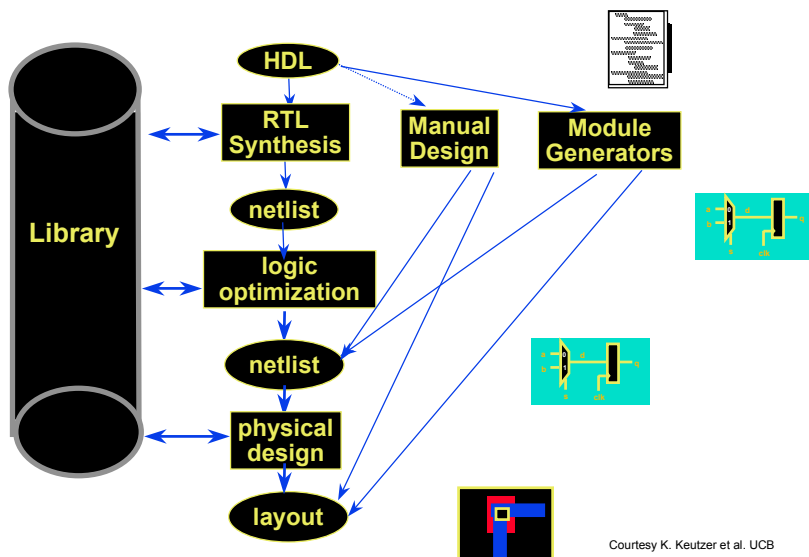
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# Routing in Integrated Circuits

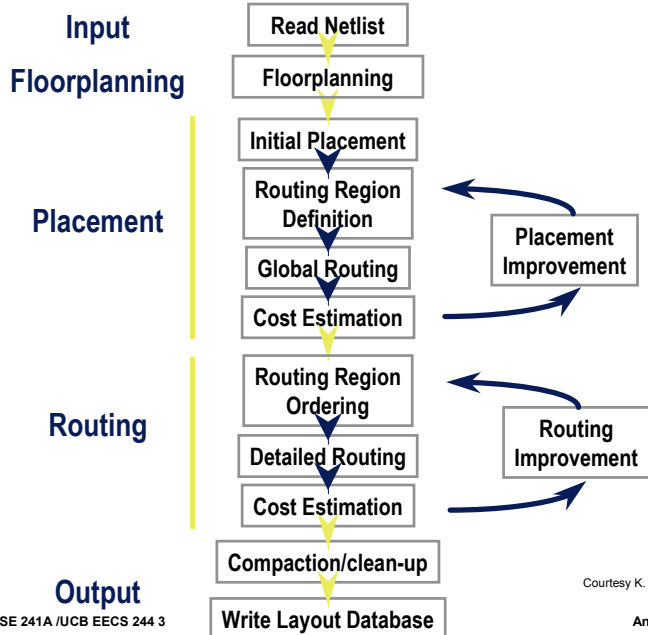
A. Kahng  
K. Keutzer  
A. R. Newton

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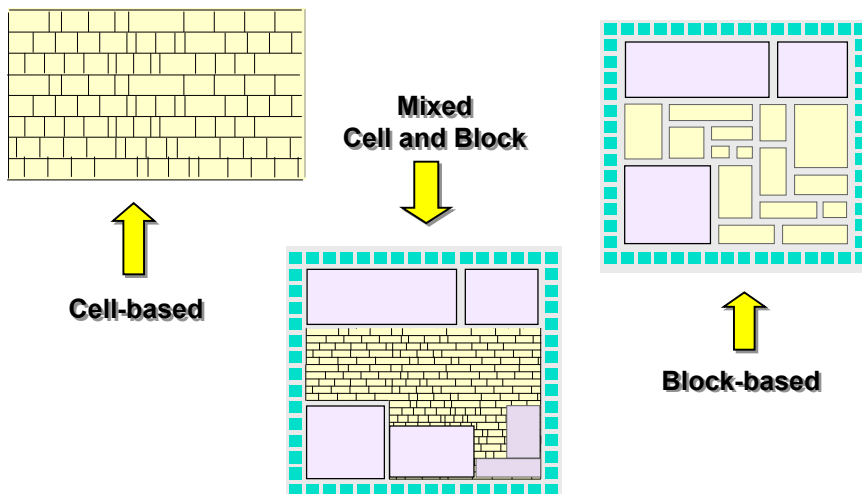
## RTL Design Flow



# Physical Design Flow



# Routing Applications



## Routing Algorithms

### ■ Global routing

- Guide the detailed router in large design
- May perform quick initial detail routing
- Commonly used in cell-based design, chip assembly, and datapath design
- Also used in floorplanning and placement

### ■ Detail routing

- Connect all pins in each net
- Must understand most or all design rules
- May use a compactor to optimize result
- Necessary in all applications

## Basic Rules of Routing - 1

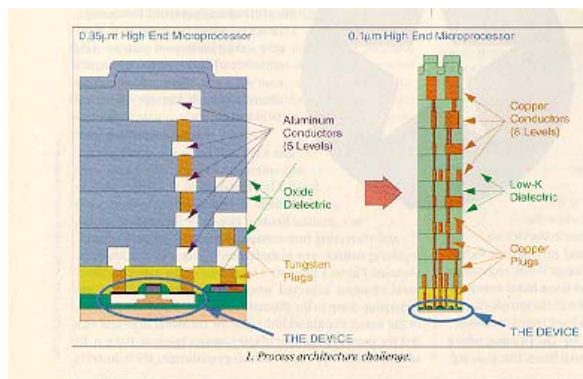
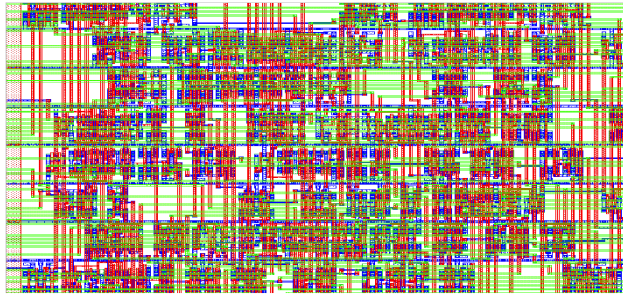


Photo courtesy:  
Jan M. Rabaey  
Anantha Chandrakasan  
Borivoje Nikolic

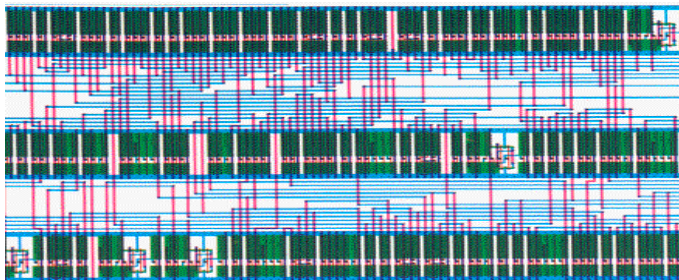
- Wiring/routing performed in layers – 5-9, typically only in “Manhattan” N/S E/W directions
  - E.g. layer 1 – N/S
  - Layer 2 – E/W
- A segment cannot cross another segment on the same wiring layer or ...?
- Wire segments *can* cross wires on other layers
- Power and ground typically have their own layers

## Basic Rules of Routing – Part 2



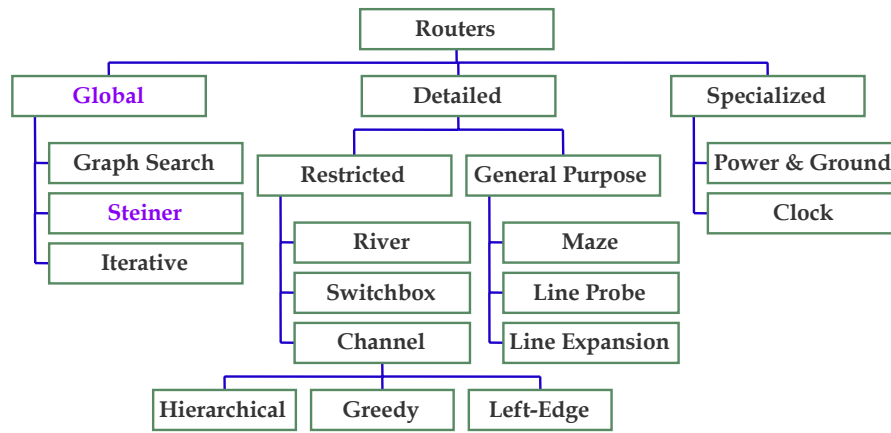
- Routing can be on a fixed grid – or gridless
- Case 1: Detailed routing over cells
  - Wiring can go over cells
  - Design of cells must try to minimize obstacles to routing – i.e. minimize use of metal-1, metal-2
  - Cells *do not* need to bring signals (i.e. inputs, outputs) out to the channel – the route will come to them

## Basic Rules of Routing – Part 3



- Routing can be on a fixed grid – or gridless
- Case 2: Detailed routing only in channels
  - Wiring can only go over a row of cells when there is a free track – can be inserted with a “feedthrough”
  - Design may use of metal-1, metal-2
  - Cells *must* bring signals (i.e. inputs, outputs) out to the channel through “ports” or “pins”

## Taxonomy of VLSI Routers



## Global Routing

### ■ Objectives

- Minimize wire length
- Balance congestion
- Timing driven
- Noise driven
- Keep buses together

### ■ Frameworks

- Steiner trees
- Channel-based routing
- Maze routing

## Global Routing Formulation

**Given** (i) Placement of blocks/cells  
(ii) channel capacities

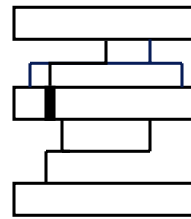
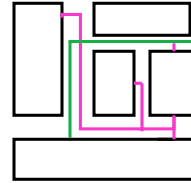
**Determine**  
Routing topology of each net

**Optimize**  
(i) max # nets routed  
(ii) min routing area  
(iii) min total wirelength

**Classic terminology:** In general cell design or standard cell design, we are able to move blocks or cell rows, so we can guarantee connections of all the nets (“variable-die” + channel routers).

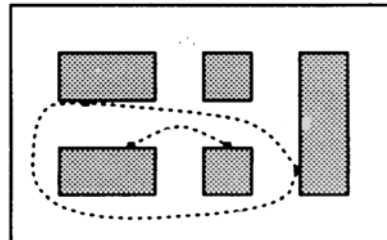
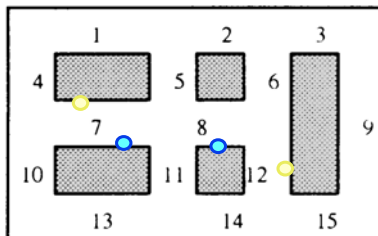
**Classic terminology:** In gate-array design, exceeding channel capacity is not allowed (“fixed-die” + area routers).

Since Tangent’s Tancell (~1986), and > 3LM processes, we use area routers for cell-based layout



## Global Routing

- Provide guidance to detailed routing (why?)
- Objective function is application-dependent

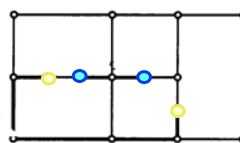
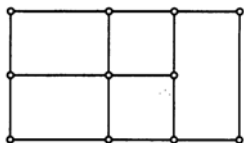
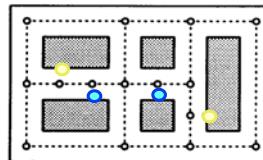
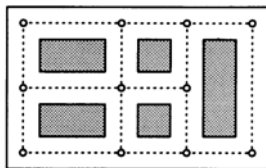


## Graph Models for Global Routing

- Global routing problem is a graph problem
- Model routing regions, their adjacencies and capacities as graph vertices, edges and weights
- Choice of model depends on algorithm
- Grid graph model
  - Grid graph represents layout as a  $h \times w$  array, vertices are layout cells, edges capture cell adjacencies, zero-capacity edges represent blocked cells
- Channel intersection graph model for block-based design

## Channel Intersection Graph

- Edges are channels, vertices are channel intersections (CI),  $v_1$  and  $v_2$  are adjacent if there exists a channel between  $(CI_1$  and  $CI_2)$ . Graph can be extended to include pins.



## Global Routing Approaches

---

- Can route nets:
  - Sequentially, e.g. one at a time
  - Concurrently, e.g. simultaneously all nets
- Sequential approaches
  - Sensitive to ordering
  - Usually sequenced by
    - Criticality
    - Number of terminals
- Concurrent approaches
  - Computationally hard
  - Hierarchical methods used

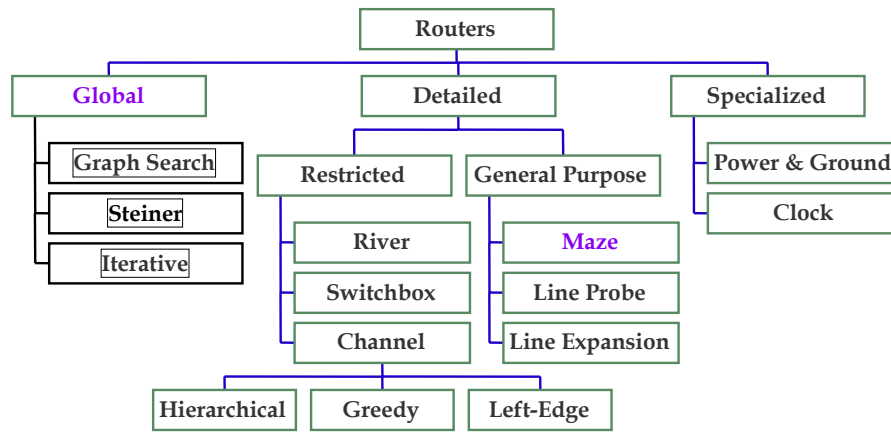
## Sequential Approaches

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- Solve a single net routing problem
- Differ depending on whether net is two- or multi-terminal
- Two-terminal algorithms
  - Maze routing algorithms
  - Line probing
  - Shortest-path based algorithms
- Multi-terminal algorithms
  - Steiner tree algorithms



## Taxonomy of VLSI Routers

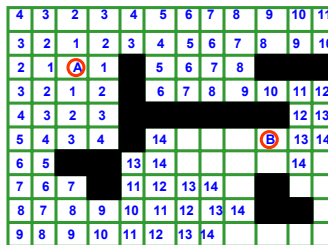


## Two-Terminal Routing: Maze Routing

- Maze routing finds a path between source (s) and target (t) in a planar graph
- Grid graph model is used to represent block placement
- Available routing areas are unblocked vertices, obstacles are blocked vertices
- Finds an optimal path
- Time and space complexity  $O(\text{height} \times \text{width})$

## Maze Routing

- Point to point routing of nets
- Route from source to sink
- Basic idea = wave propagation (Lee, 1961)
  - Breadth-first search + back-tracing after finding shortest path
  - Guarantees to find the shortest path
- Objective = route all nets according to some cost function that minimizes congestion, route length, coupling, etc.

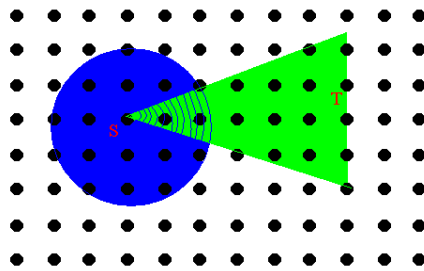


## Maze Routing

- Initialize priority queue Q, source S, and sink T
- Place S in Q
- Get lowest cost point X from Q, put neighbors of X in Q
- Repeat last step until lowest-cost point X is equal to the sink T
- Rip and reroute nets, i.e., select a number of nets based on a cost function (e.g., congestion of regions through which net travels), then remove the net and reroute it
- Main objective: reduce overflow
  - Edge overflow = 0 if num\_nets less than or equal to the capacity
  - Edge overflow = num\_nets – capacity if num\_nets is greater than capacity
  - Overflow =  $\sum$  (edge overflows) over all edges

## Maze Routing Cost Function and Directed Search

- Points can be popped from queue according to a multivariable cost function
- Cost = function(overflow, coupling, wire length, ... )
- Add <distance to sink> to cost function → directed search
  - Allows maze router to explore points around the direct path from source to sink first



S denotes the source point  
T is the sink point

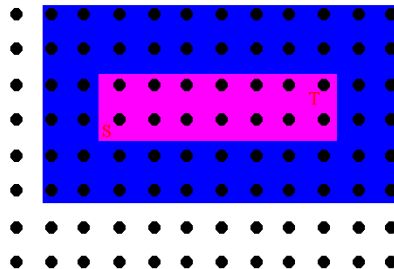
Directed search limits the search space when all other cost variables are equal

Non directed search expands in a circular fashion from S

Directed search expands in a conical fashion from S to T

## Limiting the Search Region

- Since majority of nets are routed within the bounding box defined by S and T, can limit points searched by maze router to those within bounding box
  - Allows maze router to finish sooner with little or no negative impact on final routing cost
  - Router will not consider points that are unlikely to be on the route path



S denotes the source point  
T is the sink point

Bounding box of S and T

Normally, the search region is restricted to the bounding box + X

In this example,  $X = 2$

The points outside of blue area are not considered by the maze router

## Problems With Maze Routing

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**Slow:** for each net, we have to search  $N \times N$  grid

**Memory:** total layout grid needs to be kept  $N \times N$

### Improvements

- Simple speed-up
- Minimum detour algorithm (Hadlock, 1977)
- Fast maze algorithm (Soukup, 1978)
  - depth-first search until obstacle
  - breadth-first at obstacle
  - until target is reached
- Will find a path if it exists, may be suboptimal
- Typical speed-up 10-50x

### Further improvements

- Maze routing infeasible for large chips
- Line search (Mikami & Tabuchi, 1968; Hightower, 1969)
- Pattern routing

## Line-Probe Algorithm

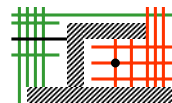
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*Mikami&Tabuchi IFIPS Proc, Vol H47, pp 1475-1478, 1968*

### Mikami+Tabuchi's algorithm

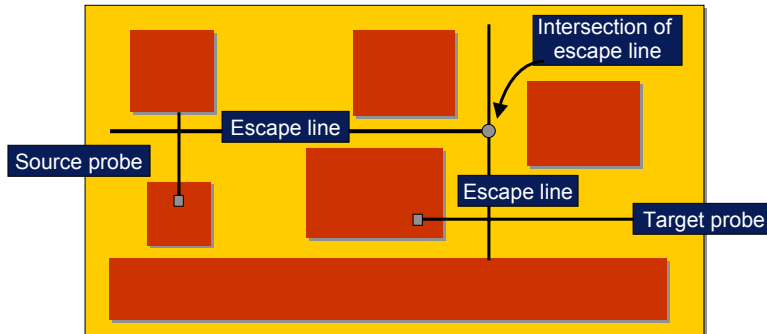
- Generate search lines from both source and target (level-0 lines)
- From every point on the level-i search lines, generate perpendicular level-(i+1) search lines
- Proceed until a search line from the source meets a search line from a target
- Will find the path if it exists, but not guaranteed to find the shortest path

Time and space complexity:  $O(L)$ , where  $L$  is the number of line segments



## Line-Probe Summary

- Fast, handles large nets / distances / designs
- Routing may be incomplete



## Problems with Sequential Routing Algorithms

### Net ordering

- Must route net by net, but difficult to determine best net ordering!
- Difficult to predict/avoid congestion

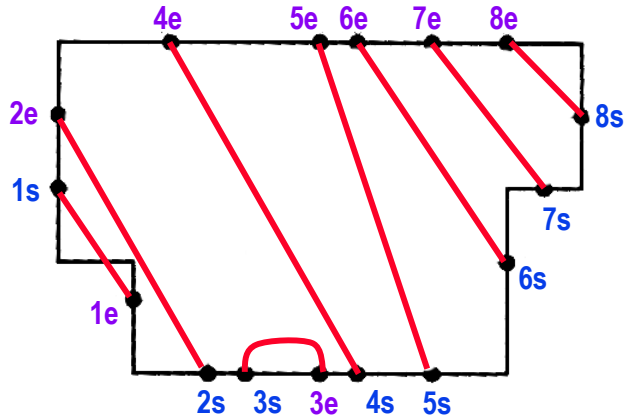
### What can be done

- Use other routers
  - Channel/switchbox routers
  - Hierarchical routers
- Rip-up and reroute



## One Layer Routing: General River-Routing

- Create circular list of all terminals ordered counterclockwise according to position on boundary



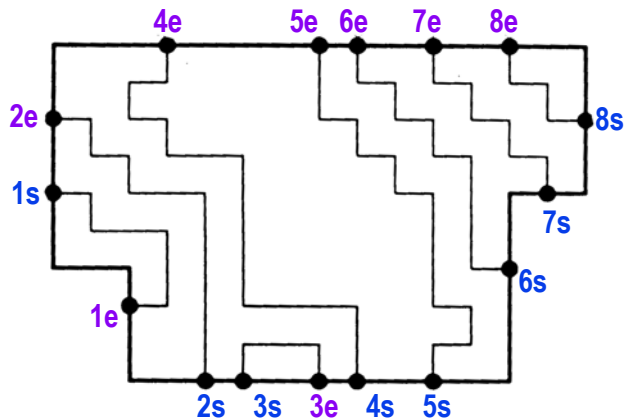
ECE 260B – CSE 241A /UCB EECS 244 29

Courtesy K. Keutzer et al. UCB

Andrew B. Kahng, UCSD

## One Layer Routing: General River-Routing

- Boundary-packed solution
- Flip corners to minimize wire length

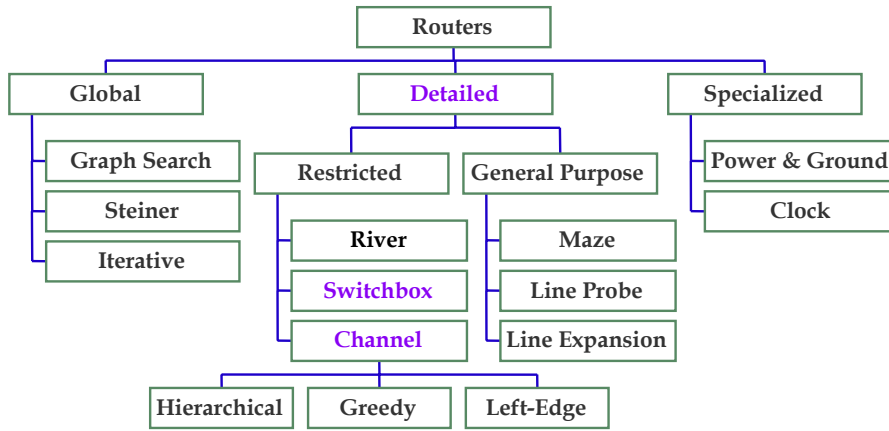


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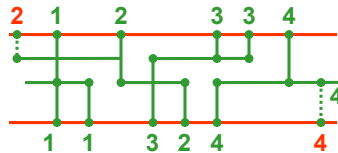
## Taxonomy of VLSI Routers



## Channel vs. Switchbox

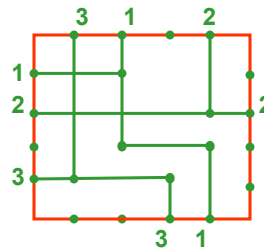
### Channel

- Channel may have exits at left and right sides, but exit positions are not fixed
- We may map exits to either lower or upper edge of a channel
- One dimensional problem



### Switch box

- Terminal positions on all four sides of a switchbox are fixed
- Two dimensional problem



**Switchbox routing is more difficult**



## Channel Routing Problem

**Input:** Pins on the lower and upper edge

**Output:** Connection of each net

**Constraints (Assumption)**

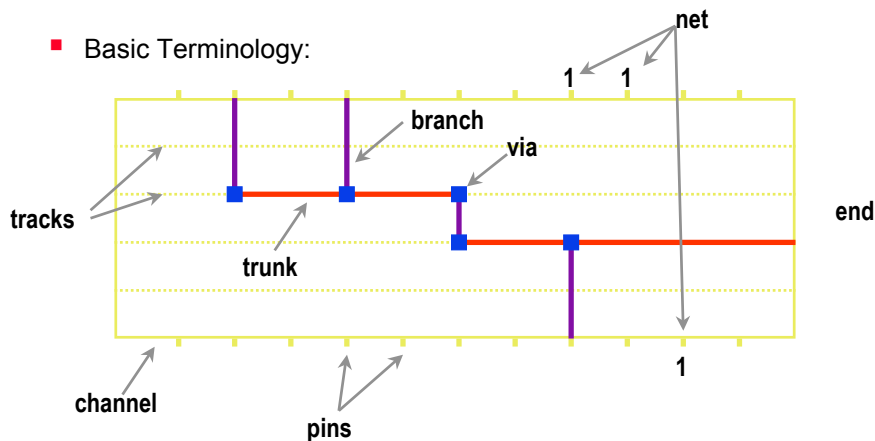
- (i) grid structure
- (ii) two routing layers. One for horizontal wires, the other for vertical wires
- (iii) vias for connecting wires in two layers

**Minimize:**

- (i) # tracks (channel height)
- (ii) total wire length
- (iii) # vias

## Channel Routing

▪ Basic Terminology:



- Fixed pin positions on top and bottom edges
- Classical channel: no nets leave channel
- Three-sided channel possible

## Channel/Switch Box Routing Algorithms

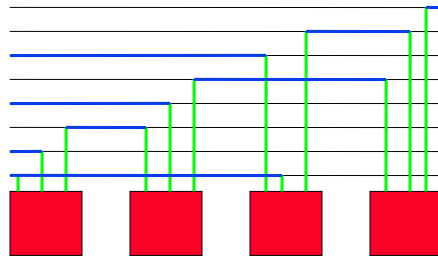
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- Graph theory based algorithm  
Yoshimura and Kuh
  - Greedy algorithm  
Rivest and Fiduccia
  - Maze routing and its variations  
Lee, Robin, Soukup, Ohtsuki
  - Hierarchical wire routing  
Burstein and Pelavin
- } Channel routing
- } Channel / switchbox and general area routing

## Trivial Channel Routing

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- Assign every net its own track

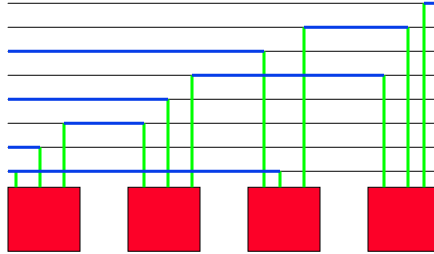


Dehon- Caltech

## Trivial Channel Routing

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- Assign every net its own track
  - Channel width  $> N$  (single output functions)
  - Chip bisection  $\propto N \rightarrow$  chip area  $N^2$

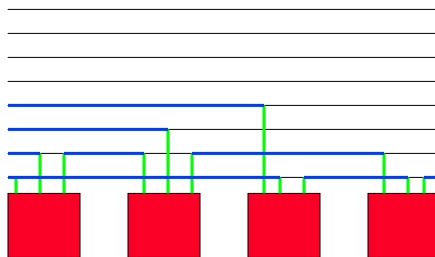


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## Sharing Tracks

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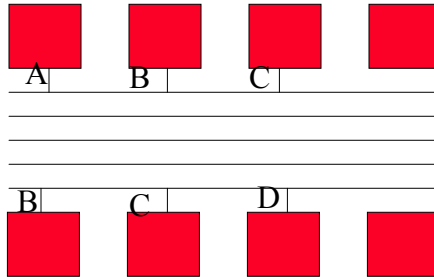
- Want to Minimize tracks used
- Trick is to share tracks



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## Not that Easy

- With Two sides
  - Even assigning one track/signal may not be enough

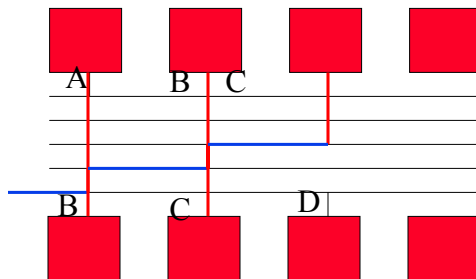


Dehon- Caltech

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Dehon- Caltech

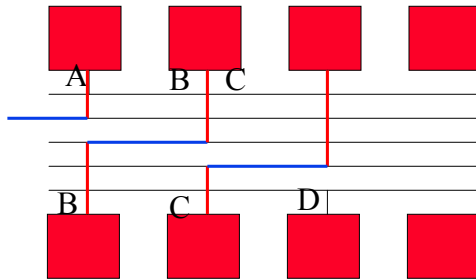


Bad  
assignment  
Overlap:  
A,B  
B,C

## Not that Easy

Dehon- Caltech

- With Two sides
  - Even assigning one track/signal may not be enough

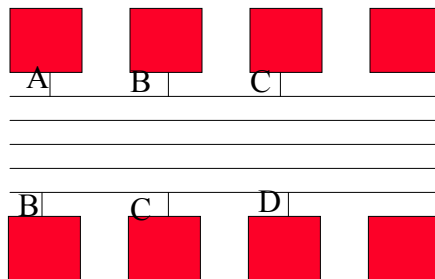


Valid assignment  
avoids overlap

## Not that Easy

Dehon- Caltech

- With Two sides
  - Even assigning one track/signal may not be enough



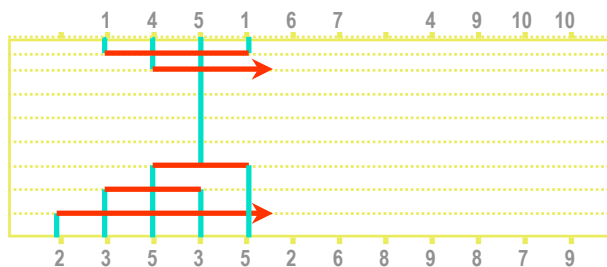
There are vertical  
constraints on  
ordering

## Greedy Channel Router

*R.L. Rivest and C.M. Fiduccia " A Greedy Channel Router", 19th DAC, 1982 P418-424*

- ☞ A simple linear time algorithm
- ☞ Guarantee the completion of all the nets (may extend to right-hand side of the channel)
- ☞ Produce both restricted doglegs and unrestricted doglegs

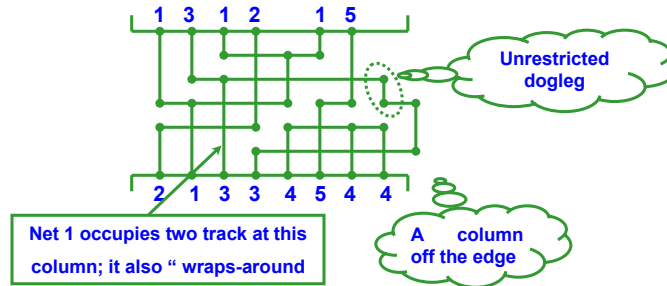
## Greedy Router: Rivest & Fiduccia



- Proceed column by column (left to right)
- Make connections to all pins in that column
- Free up tracks by collapsing as many tracks as possible to collapse nets
- Shrink range of rows occupied by a net by using doglegs
- If a pin cannot enter a channel, add a track
- $O(\text{pins})$  time

## Comments on Greedy Router (Rivest&Fiduccia 1982)

- ☞ Always succeeds (even if cyclic conflict is present);
- ☞ Allows unrestricted doglegs;
- ☞ Allows a net to occupy more than 1 track at a given column;
- ☞ May use a few columns off the edge;



## Overview of Greedy Router

### Left-to-right, Column-by-column scan

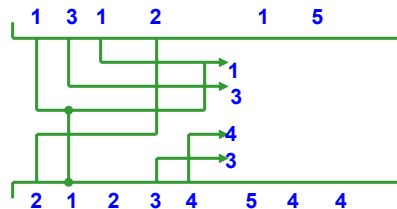
```

c:=0;
while (not done) do
  begin
    c:=c+1;
    complete wiring at column c;
  end;

```

### In general, at a point in a net may be

- (1) empty (net 5)
- (2) unsplit (nets 1,4)
- (3) split (net 3)
- (4) completed (net2)



## Parameters to Greedy Router

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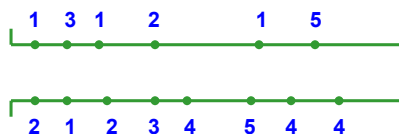
- ☞ Initial-channel-width    icw
- ☞ Minimum-jog-length    mjl (Why?)
- ☞ Steady-net-constant    snc
- ☞ Usually start icw as d. the density
- ☞ Mjl controls the number of vias, use a large mjl for fewer vias
- ☞ Snc also controls # of vias (typical value=10 Why?)

## Operations at Each Column

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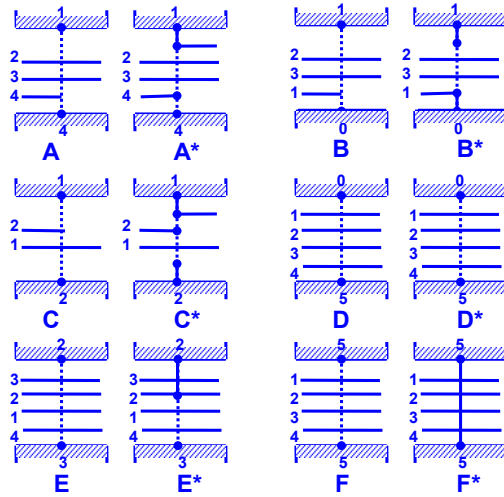
At each column, the greedy router tries to maximize the utility of the wiring produced:

- A:** Make minimal feasible top/bottom connections;
- B:** Collapse (**connect**) split nets;
- C:** Move split nets closer to one another;
- D:** Raise rising nets/lower falling nets, i.e. bring nets closer to destination terminal;
- E:** Widen channel when necessary;
- F:** Extend to next column;

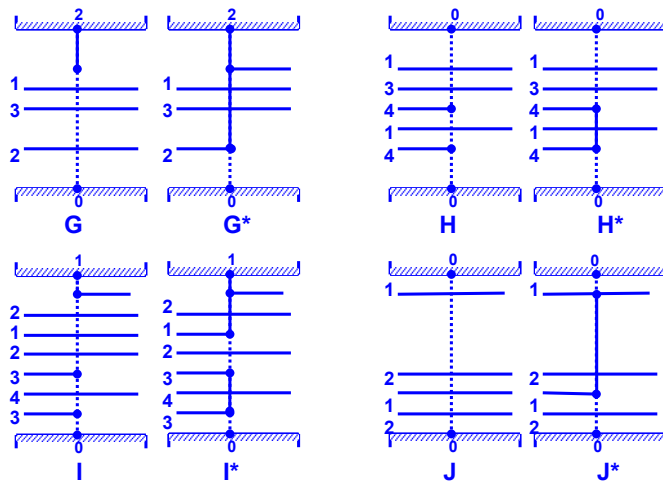




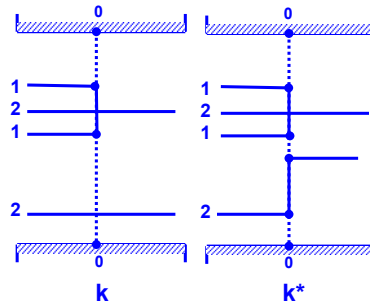
## (A) Make Minimal Feasible top/bottom Connections



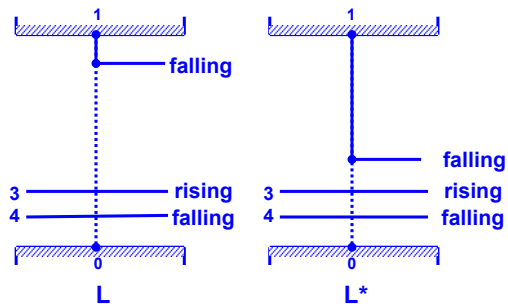
## (B) Collapse/(Connect) Split Nets



## ( C ) Move Split Nets Closer

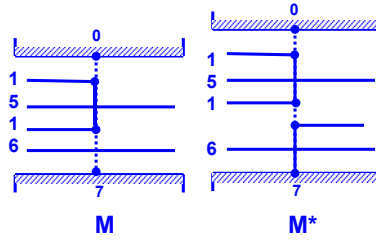


## (D) Rising/Falling



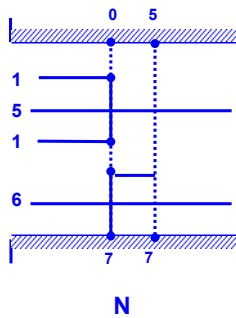
## (E) Insert New Track

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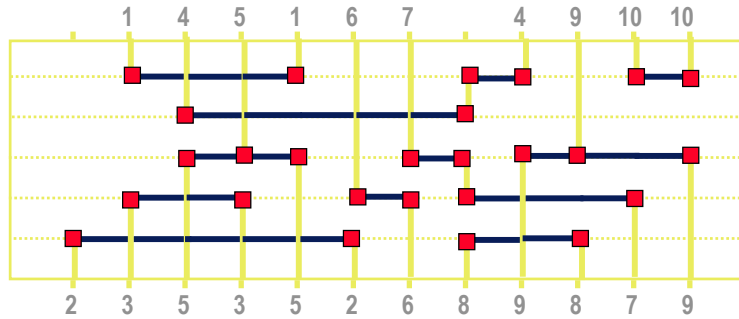


## (F) Extend to Next Column

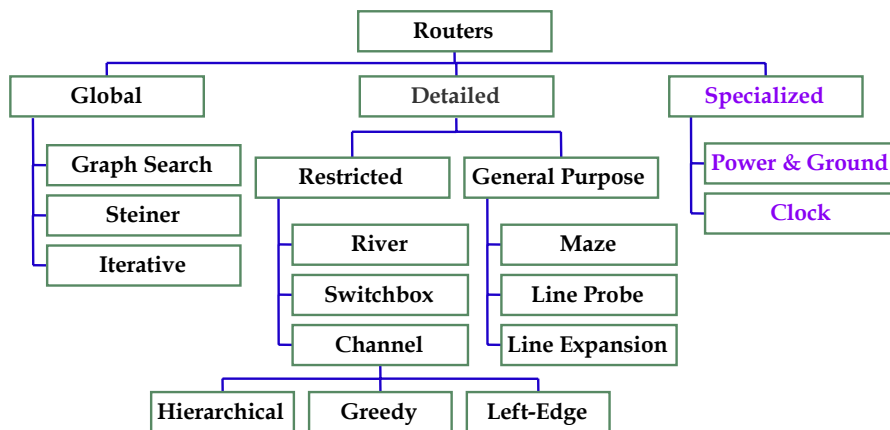
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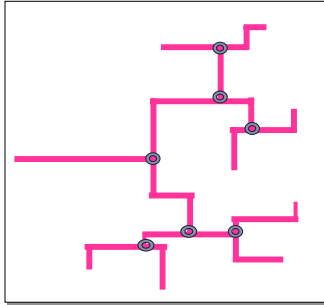
## Greedy Routing Example



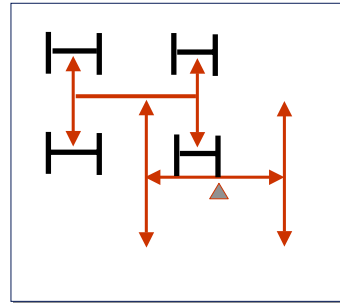
## Taxonomy of VLSI Routers



## Clock Routing Structures



Balanced Tree

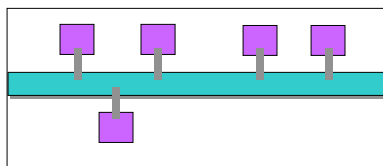


H-Tree

Or in low performance ASIC designs a clock may be  
"just another net"

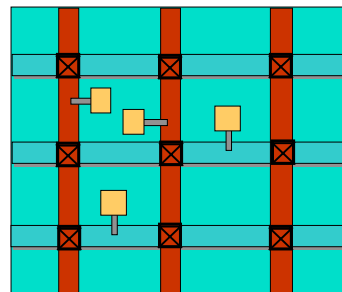
## Clock Routing

- Multiple Clock Domains



← Trunk or Grid

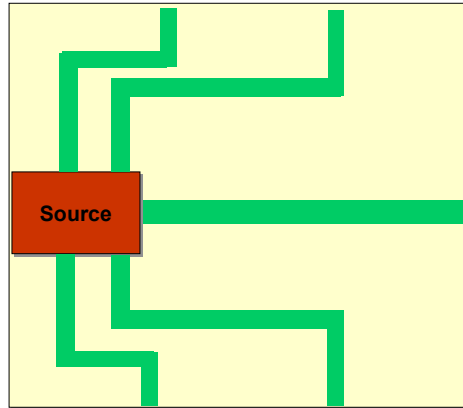
Clock Mesh →



## Power Routing

- Power Mesh
- Power Ring
- Star Routing

Star Routing →

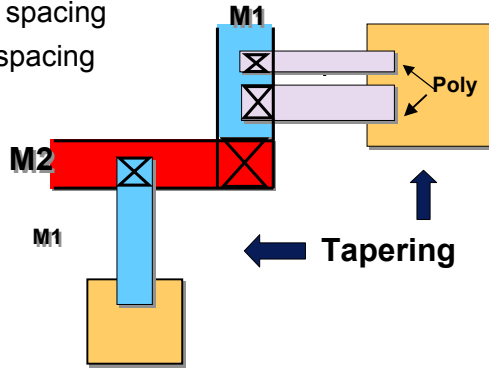


In cases where an entire layer is devoted to power, both N/S, E/W directions may be used.

## A Potpourri of Other Routing Issues

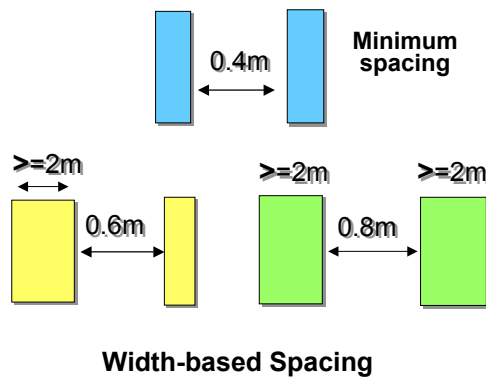
## Detailed Routing Issues

- Routing completion
- Width and spacing rule
  - Minimum width and spacing
  - Variable width and spacing
    - Connection
    - Net
    - Class of nets
  - Tapering



## Detailed Routing Issues

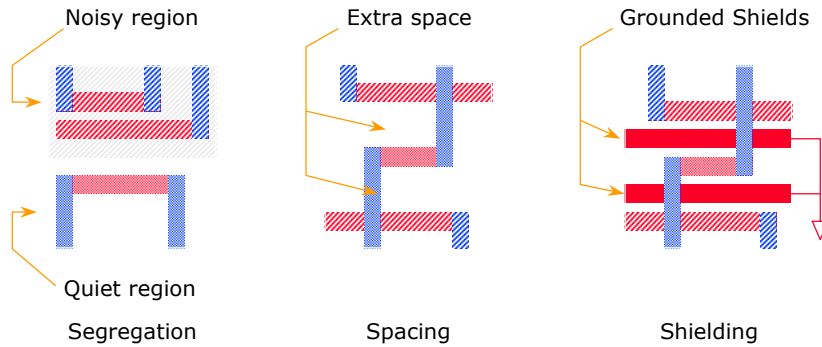
- Width and spacing rule



Width-based Spacing

## Detailed Routing Issues

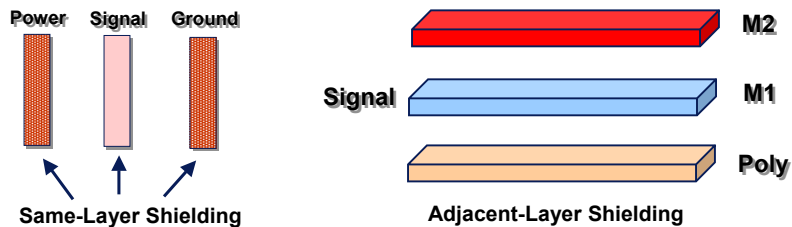
### • Noise-driven



## Detailed Routing Issues

### • Shielding

- Same-layer shielding
- Adjacent-layer shielding

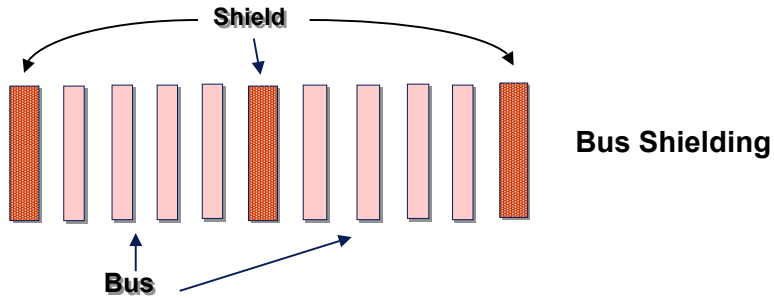




## Detailed Routing Issues

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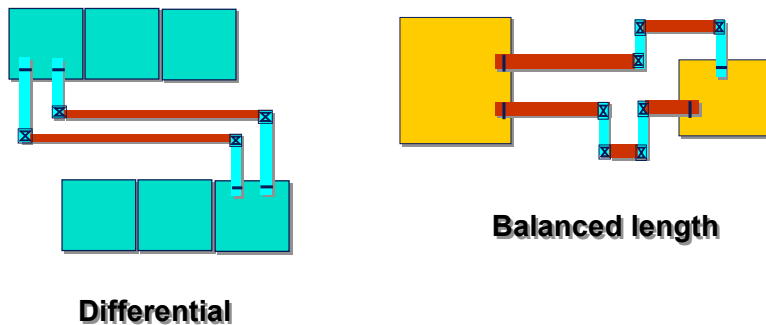
- Shielding
  - Bus shielding
  - Bus interleaving



## Detailed Routing Issues

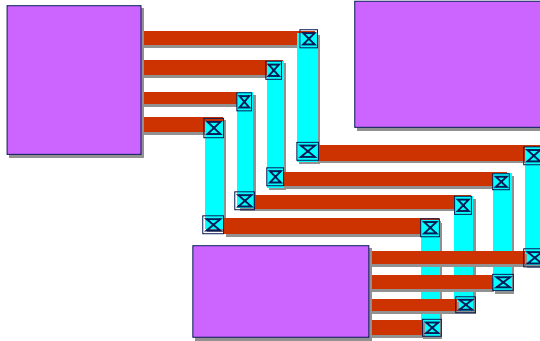
---

- Differential pair routing
- Balanced length or capacitance



## Detailed Routing Issues

- **Bus Routing**



## Detailed Routing Objectives

- Process antenna rule
- Phase shift mask
- Other manufacturability objectives

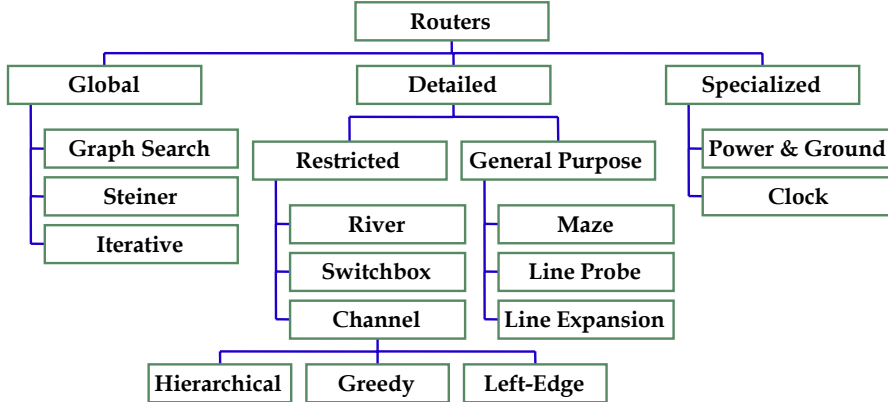
## Incremental Routing

- Re-route with minor local adjustment
- Need rip-up and reroute capability
- Difficult to confine perturbation when compactor is used

## Current Status

- Routing is not a “showstopper” in current VLSI designs
- But ... routing is a perennial bottleneck, and therefore there's at least one new start-up every year
- Focus of start-ups is:
  - Chip-level routing for assembly
  - Special purpose niche routing – e.g. die to bonding pads

## Routing Summary



Routing requires an especially large toolbox of techniques

Every router mentioned here is used

## Summary

- Large toolset → many algorithms
- Fortunately, most of the algorithms are simple
- Be sure you're familiar with:
  - Maze Routing – Lee
  - Line routing - Hightower
  - Single-layer switchbox routing
  - Greedy channel routing - Rivest
- Be familiar with the flow and relationship between routers

## Extras

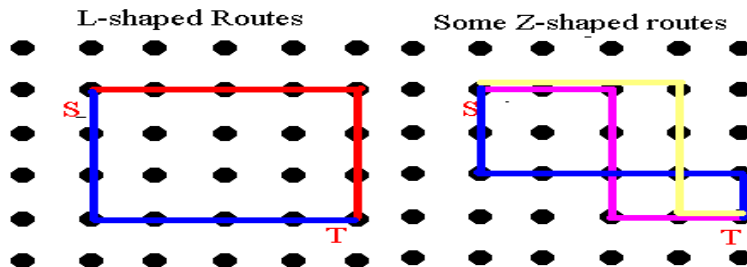
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- Pattern-based routing
- Steiner Trees
- Concurrent global routing
- Yoshimura-Kuh
- Compaction
- Other Physical Issues

## Pattern-Based Routing

---

- Restrict routing of net to certain basic templates
- Basic templates are L-shaped (1 bend) or Z-shaped (2 bends) routes between a source and sink
- Templates allow fast routing of nets since only certain edges and points are considered



## Steiner Trees

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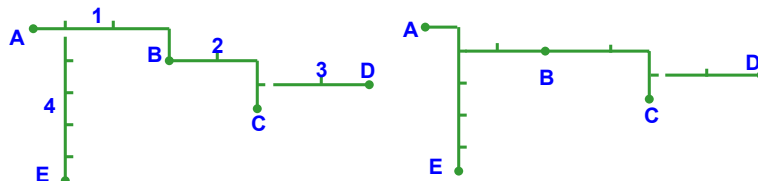
## Connecting Multi-Terminal Nets

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In general, maze and line-probe routing are not well-suited to multi-terminal nets

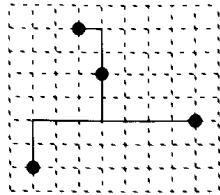
Several attempts made to extend to multi-terminal nets

- Connect one terminal at a time
- Use the entire connected subtrees as sources or targets during expansion
- Ripup/Reroute to improve solution quality (remove a segment and re-connect)

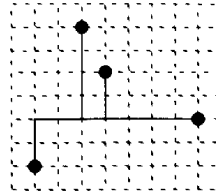


- Results are sub-optimal
- Inherit time and memory cost of maze and line-probe algorithms

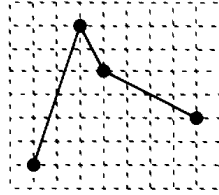
## Multi-terminal Nets: Different Routing Options



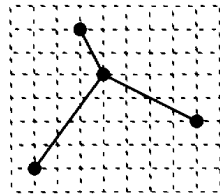
(a) Steiner Tree (14)



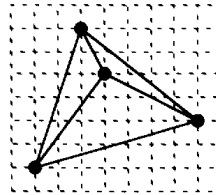
(b) Steiner Tree with Trunk (15)



(d) Chain (17)



(c) Minimum Spanning Tree (16)



(e) Complete Graph (42)

Cost is determined by routing model

## Steiner Tree Based Algorithms

- Tree interconnecting a set of points (demand points,  $D$ ) and some other (intermediate) points (Steiner points,  $S$ )
- If  $S$  is empty, Steiner Minimum Tree (SMT) equivalent to Minimum Spanning Tree (MST)
- Finding SMT is NP-complete; many good heuristics
  - SMT typically 88% of MST cost; best heuristics are within  $\frac{1}{2}$  % of optimal on average
- Underlying Grid Graph defined by intersection of horizontal and vertical lines through demand points (Hanan grid)  $\rightarrow$  Rectilinear SMT and MST problems
- Can modify MST to approximate RMST, e.g., build MST and rectilinearize each edge

## Minimum Spanning Tree (Prim's construction)

Given a weighted graph  
Find a spanning tree whose weight is minimum

### Prim's algorithm

start with an arbitrary node  $s$

$T \leftarrow \{s\}$

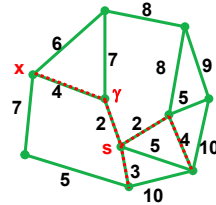
while  $T$  is not a spanning tree

{ find the closest pair  $x \in V-T, y \in T$   
add  $(x,y)$  to  $T$

runs in  $O(n^2)$  time

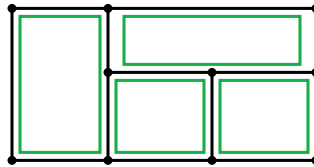
very simple to implement

always gives a tree of minimum cost

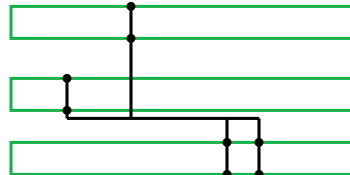


## Applying Spanning and Steiner Tree Algorithms

- General cell/block design: channel intersection graphs



- Standard-cell or gate-array design: RSMT or RMST in geometry or grid-graph





## Concurrent Global Routing

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## Global Routing: Concurrent Approaches

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- Can formulate routing problem as *integer programming*, solve simultaneously for all nets

### Given

- (i) Set of Steiner trees for each net
- (ii) Placement of blocks/cells
- (iii) Channel capacities

### Determine

Select a Steiner tree for each net w/o violating channel capacities

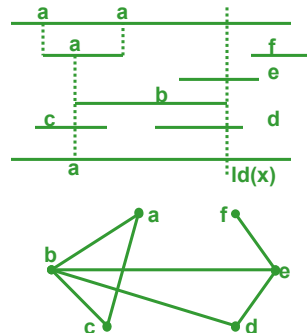
### Optimize

Min total wirelength

# Yoshimura and Kuh

## Horizontal Constraint Graph (HCG)

1. Node  $v_i$ : represents a horizontal interval spanned by net  $i$
2. There is an edge between  $v_i$  and  $v_j$  if horizontal intervals overlap
3. No two nets with a horizontal constraint may be assigned to the same track
4. Maximum clique of HCG establishes lower bound on # of tracks: # tracks  $\geq$  size of maximum clique of HCG



Local density at column  $C$ ,  $ld(C) = \#$  nets split by column  $C$

Channel Density  $d = \max ld(C)$  over all  $C$

Each net spans over an interval

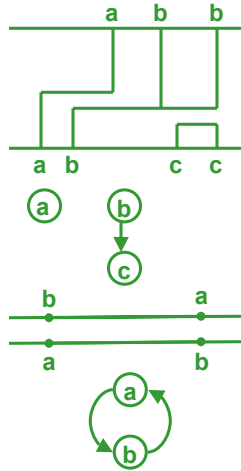
**Horizontal Constraint Graph (HCG)** is an *undirected* graph with:

vertex : net

edge:  $\langle n_j, n_k \rangle$ , if intervals  $I_j, I_k$  intersect

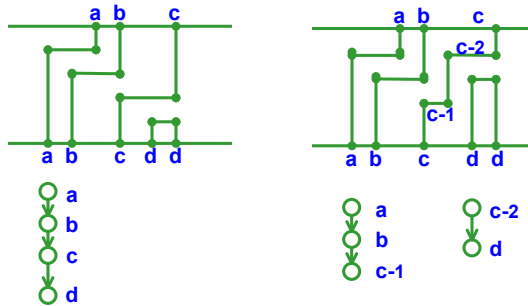
# Vertical Constraint Graph (VCG)

1. Node: represents a net
2. Edge ( $a_1 \rightarrow a_2$ ) exists if at some column:
  - Net  $a_1$  has a terminal on the upper edge
  - Net  $a_2$  has a terminal on the lower edge
  - Edge  $a_1 \rightarrow a_2$  means that Net  $a_1$  must be above Net  $a_2$
3. Establishes lower bound: # tracks  $\geq$  longest path in VCG
4. VCG may have a cycle !

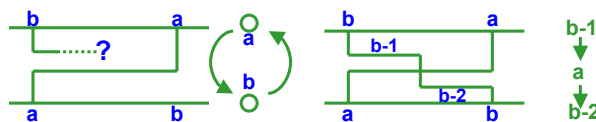


# Doglegs in Channel Routing

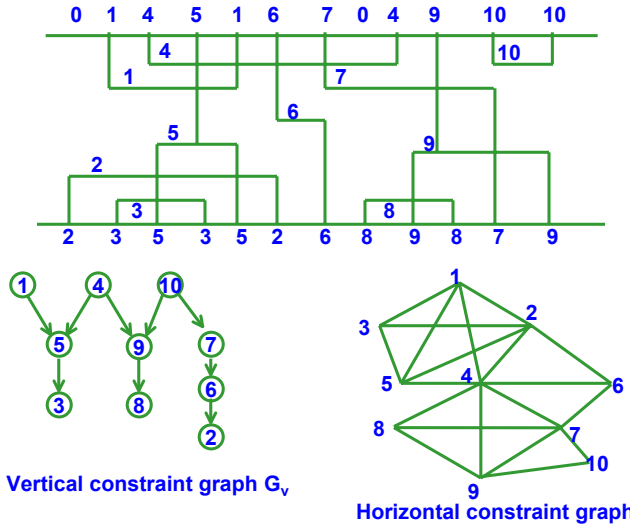
Doglegs may reduce the longest path in VCG



Doglegs break cycles in VCG



# Characterizing the Channel Routing Problem



Channel routing problem is completely characterized by the vertical constraint graph and the horizontal constraint graph.

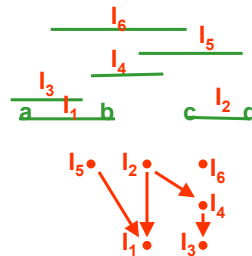
# Interval Packing

**Theorem** A set of intervals with density  $d$  can be packed into  $d$  tracks.

**Proof:**  $I_1=(a,b)$   $I_2=(c,d)$

**Define:**  $I_1 < I_2$  iff  $b < c$  or  $I_1 = I_2$

1. reflexive:  $I_1 < I_1$
2. anti-symmetric:  $I_1 < I_2, I_2 < I_1 \rightarrow I_1 = I_2$
3. transitive:  $I_1 < I_2, I_2 < I_3 \rightarrow I_1 < I_3$



Set of intervals with binary relation  $<$  forms a partially ordered set (POSET)

Intervals in a single track  $\rightarrow$  form a chain

Intervals intersecting a common column  $\rightarrow$  form an antichain

**Dilworth's theorem (1950):** If the maximum antichain of a POSET is of size  $d$ , then the POSET can be partitioned into  $d$  chains

## Left-Edge Algorithm for Interval Packing

**Repeat**

create a new track  $t$

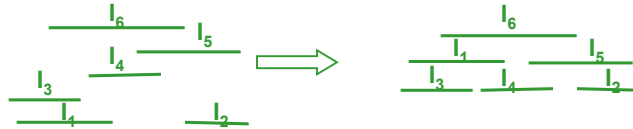
**Repeat**

put leftmost feasible interval to  $t$

**until** no more feasible interval

**until** no more interval

Intervals are sorted according to their left endpoints



$O(n \log n)$  time algorithm. **Greedy algorithm works!**

## Horizontal Constraint Graph (HCG)

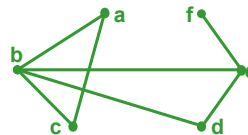
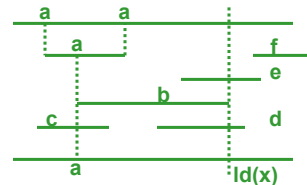
⊕ Node  $v_i$ : represents a horizontal interval spanned by net  $i$

⊕ There is an edge  $b/w$   $v_i$  and  $v_j$  if horizontal intervals overlap

⊕ No two nets with a horizontal constraint may be assigned to the same track

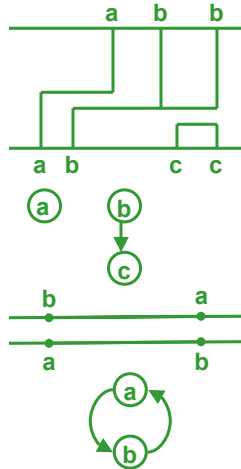
⊕ Maximum clique of HCG establishes a lower bound on # of tracks:

# tracks  $\geq$  maximum clique of HCG



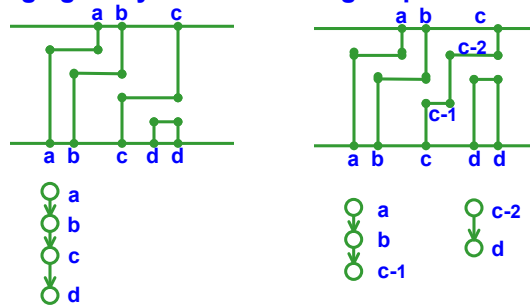
# Vertical Constraint Graph (VCG)

- Node: represents a net
- edge ( $a1 \rightarrow a2$ ): if at some column, net a1 has a terminal on the upper edge and net a2 has a terminal on the lower edge  
 $a1 \rightarrow a2$  means that net a1 has to be above a2
- Establishes a lower bound:  
 $\# \text{ tracks} \geq \text{longest path in VCG}$
- VCG may have a cycle !

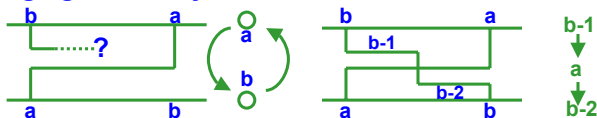


# Doglegs in Channel Routing

- Doglegs may reduce the longest path in VCG

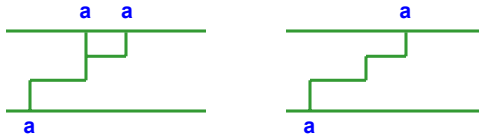


- Doglegs break cycles in VCG



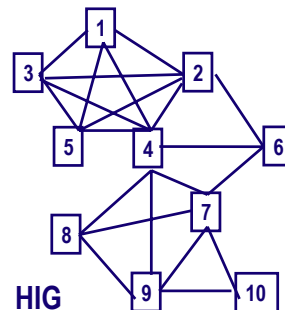
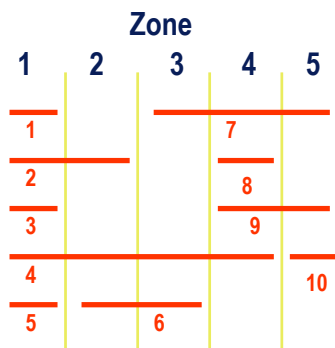
## Doglegs in Channel Routing (Cont'd)

### Restricted Dogleg vs unrestricted dogleg

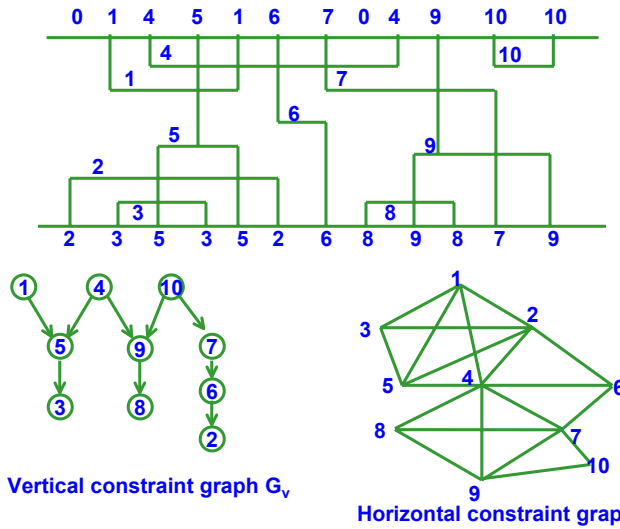


## Constraint Graph Based Algorithm: “Merging of Nets” (Yoshimura & Kuh)

- On the assumption of no cyclic constraints, nets that can be placed on the same track can be merged in the VCG, simplifying the VCG.
- Nets can be organized into zones, further simplifying the problem

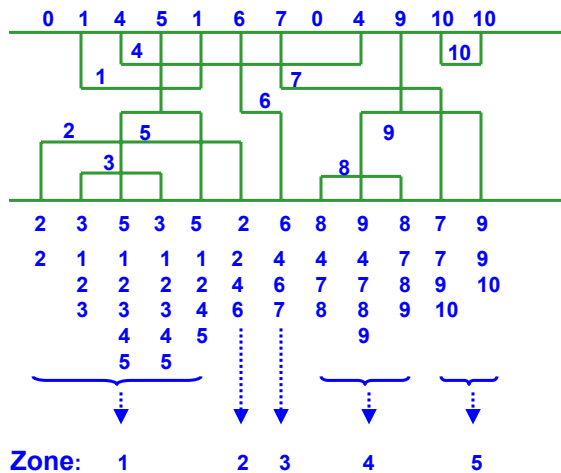


## Characterizing Channel Routing Problem



The channel routing problem is completely characterized by the vertical constraint graph and the horizontal constraint graph.

## Zone Representation of Horizontal Segments



Zones are maximum cliques in the horizontal interval graph.  
Each net *must* be routed on a different track.



## Merging of Nets

- Definition: Let  $i$  and  $j$  be nets for which the following holds:

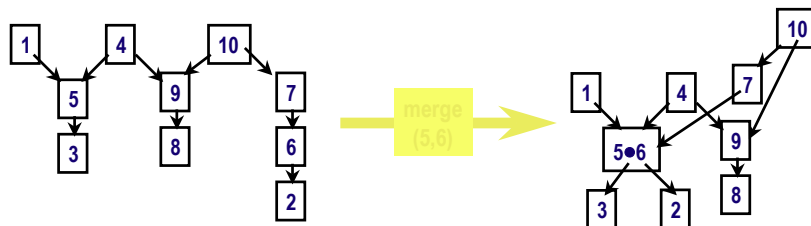
- $i$  and  $j$  are not adjacent in the HIG
- There is no direct path between  $i$  and  $j$  in the VCG

Then these nets can be assigned to the same track and hence they can be merged in the VCG

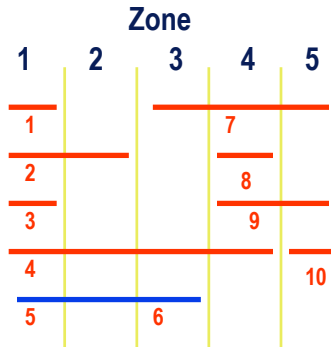
- Merging Operation:

- Combine nodes  $i$  and  $j$  into node  $i \bullet j$  in VCG
- Update zone representation such that  $i \bullet j$  occupies zones of  $i$  and  $j$

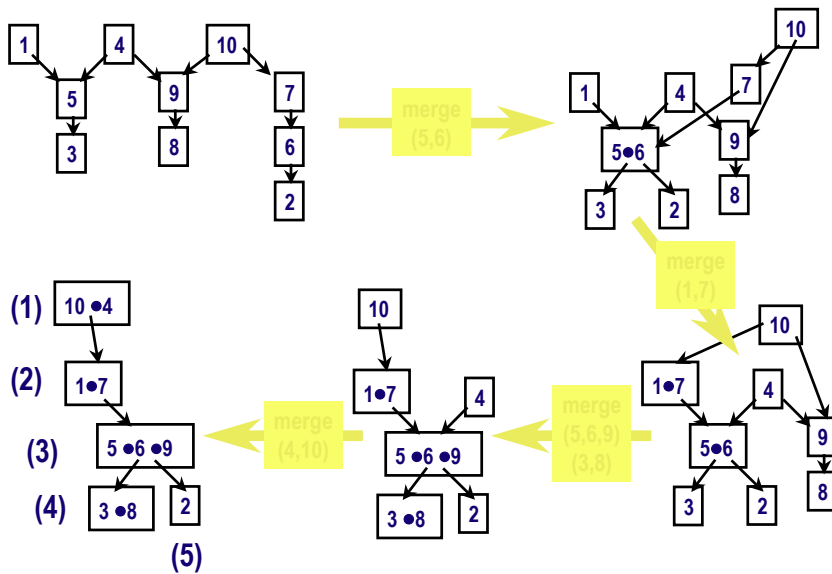
## Merging of Nets: Example



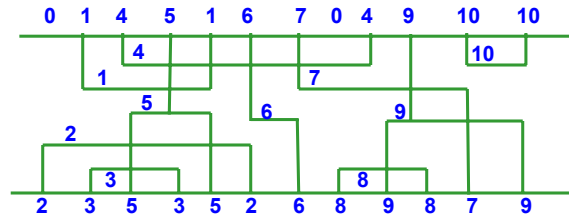
## Updating of Zone Representation



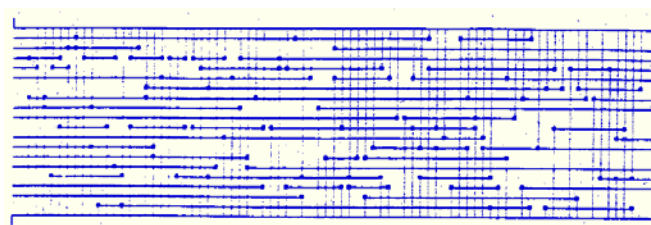
## Merging of Nets: Example



## Final Routing

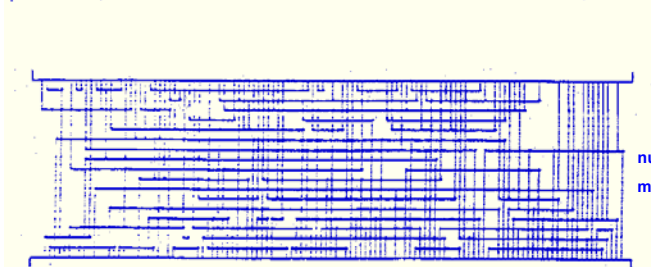


## Routing Examples by Y-K's Algorithm



number of tracks=18  
maximum density =18

Example 3c

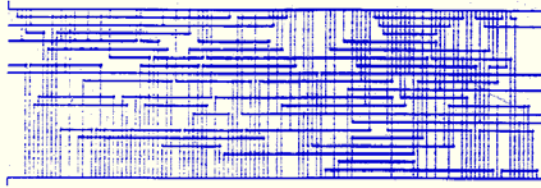


number of tracks=17  
maximum density =17

Example 4b

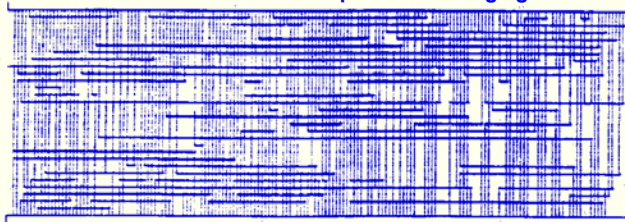
## Routing Examples by Y-K's Algorithm (Cont'd)

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number of tracks=20  
maximum density =20  
Example 5

Deutsch's Difficult example without dogleg



number of tracks=28  
maximum density =19

## Yoshimura and Kuh's Method

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### Source:

“Efficient Algorithms for Channel Routing”

by T. Yoshimura and E. Kuh

*IEEE Trans. On Computer-Aided Design of Integrated Circuits and Systems.*

Vol. CAD-1, pp25-35, Jan 1982

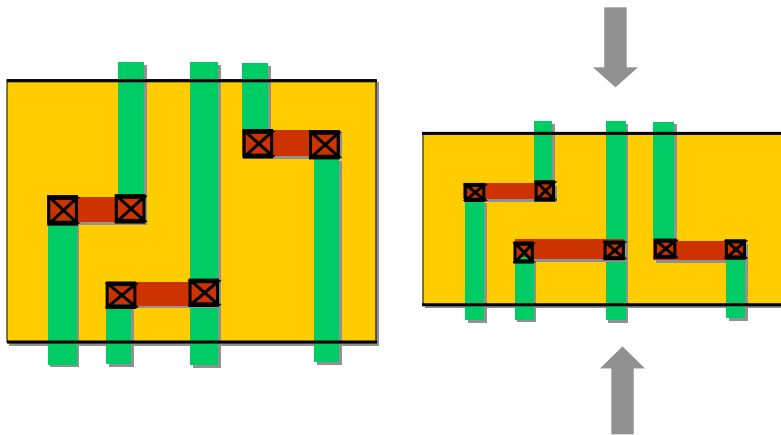
## Compaction

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## Compaction

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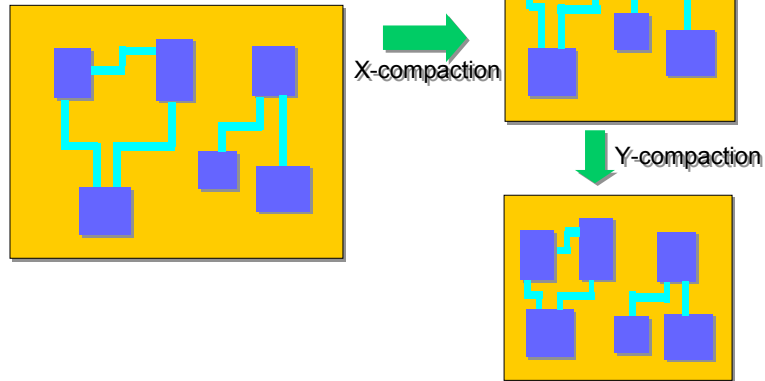
- **Channel Compaction** ( one dimension)



## Compaction

- **Area Compaction (1.5 or 2 dimension)**

- May need a lot of constraints to get desired results



## Shape-based Routing

- Evolve from maze routing
- Gridless: look at actual size of each shape
- Each shape may have its spacing rule
- Good for designs with multiple width/spacing rules and other complex rules
- Slower than gridded router



## Other Physical Issues

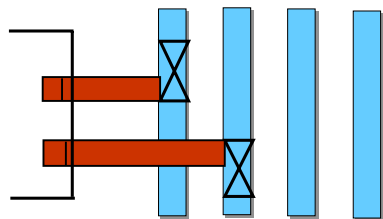
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## Detailed Routing Objectives

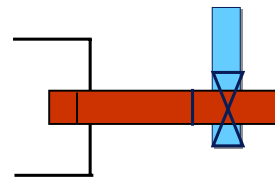
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### ■ Via selection

- Via array based on wire size or resistance
- Rectangular via rotation and offset



Rotate and offset horizontal vias



No rotation for a "cross" via

## Detailed Routing Objectives

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- Understand complex pin & equivalent pin modeling

